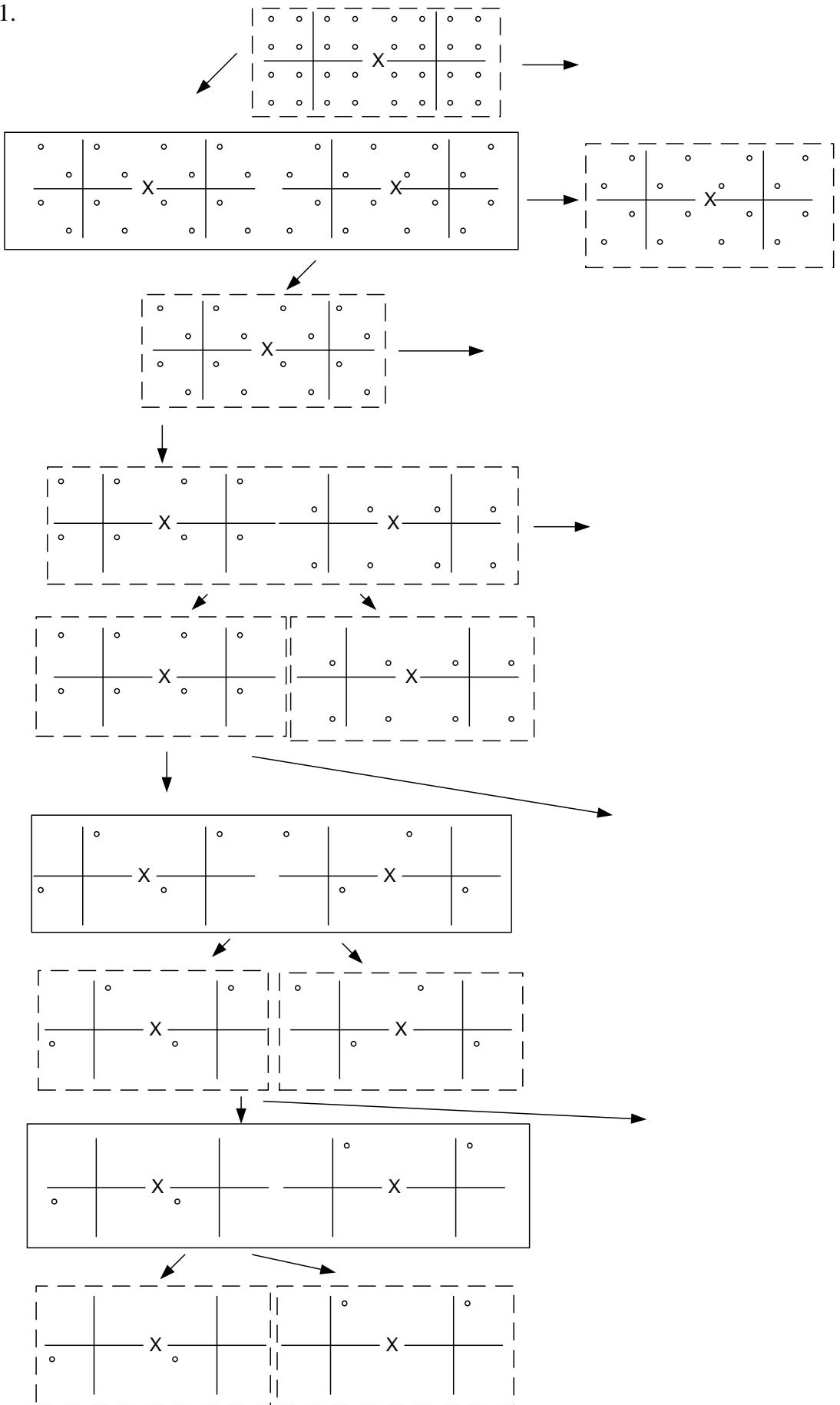


2007 Advanced Coding Theorem Hw3 solution

1.



2.

$$\underline{S}_1 \oplus \underline{S}_2 = \left\{ \begin{pmatrix} 0 \\ 0 \\ 1 \\ 1 \\ 0 \end{pmatrix}, \begin{pmatrix} 1 \\ 0 \\ 1 \\ 0 \\ 0 \end{pmatrix}, \begin{pmatrix} 0 \\ 1 \\ 0 \\ 0 \\ 1 \end{pmatrix}, \begin{pmatrix} 1 \\ 0 \\ 0 \\ 0 \\ 0 \end{pmatrix}, \begin{pmatrix} 0 \\ 1 \\ 1 \\ 0 \\ 0 \end{pmatrix} \right\}$$

$$\Delta_1 \quad \Delta_2 \quad \Delta_0 \quad \Delta_4 \quad \Delta_2$$

For table III

$$\Delta_1^2 + \Delta_2^2 + \Delta_0^2 + \Delta_4^2 + \Delta_2^2 = 8.102$$

For table IV

$$\Delta_1^2 + \Delta_2^2 + \Delta_0^2 + \Delta_4^2 + \Delta_2^2 = 8.686$$

For table V

$$\Delta_1^2 + \Delta_2^2 + \Delta_0^2 + \Delta_4^2 + \Delta_2^2 = 6.686$$

There is no other case better than above

\therefore table IV is best for $\underline{S}_1 \oplus \underline{S}_2$

3.

(1) CER 級為 1.5. , rate : 7 bits / 2D

$$\Rightarrow \text{total constellation} = 2^7 \cdot 1.5 = 192$$

$$T = \frac{16}{2} = 8$$

① for $M=8$:

$$\frac{192}{8} = 24 \text{ points per region}$$

\Rightarrow 由 encode 4 unshaped bits / 2D.

$$\text{total shaped bits} : (7-4) \cdot 8 = 24$$

$$\text{but } 8^8 = 2^{24} \Rightarrow \text{no shaping gain}$$

② for $M=7$:

$$\frac{192}{7} = 27.4 \text{ points per region}$$

\Rightarrow 由 encode 4 unshaped bits / 2D

$$\text{total shaped bits} : (7-4) \cdot 8 = 24$$

$\Rightarrow 7^8 < 2^{24}$ 可挑選的數目大過於
實際存在的組合故。

③ for $M=6$:

$$\frac{192}{6} = 32 \text{ points per region}$$

\Rightarrow 由 encode 5 unshaped bits / 2D

$$\text{total shaped bits} : (7-5) \cdot 8 = 16$$

$$\Rightarrow 6^8 > 2^{16} \text{ 有 shaping gain.}$$

i. Max. value of M : 6

for each shaping block:

16 bits for shaping.

40 unshaped bits.

(2)

1

$$\begin{array}{lll}
 g_2(0) = 1 & g_4(0) = 1 & g_8(0) = 1 \\
 g_2(1) = 2 & g_4(1) = 4 & g_8(1) = 8 \\
 g_2(2) = 3 & g_4(2) = 10 & g_8(2) = 36 \\
 g_2(3) = 4 & g_4(3) = 20 & g_8(3) = 120 \\
 g_2(4) = 5 & & \\
 g_2(5) = 6 & & \\
 \vdots & & \\
 \end{array}$$

ii

$$\begin{array}{c}
 \text{total cost} \\
 = 0
 \end{array} \left\{ \begin{array}{l} g_8(0) = 1 \end{array} \right.$$

$$\begin{array}{c}
 = 1
 \end{array} \left\{ \begin{array}{l} g_8(1) = 8 \\ \therefore \text{total cost} = 3 \end{array} \right.$$

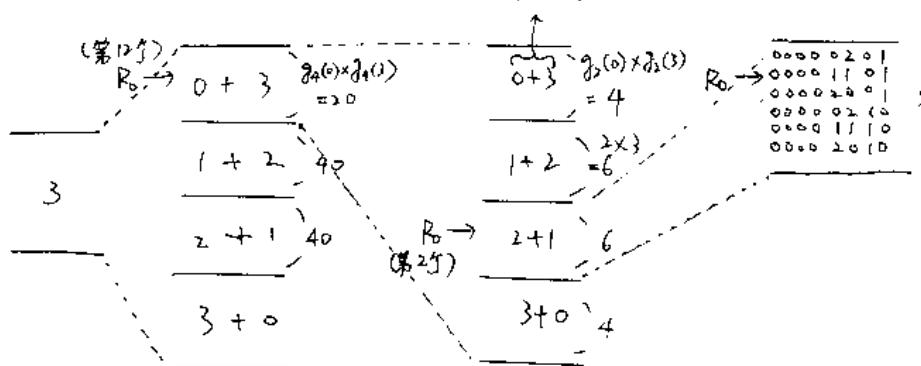
$$\begin{array}{c}
 = 2
 \end{array} \left\{ \begin{array}{l} g_8(2) = 36 \end{array} \right.$$

$$R_0 = 56 \rightarrow \begin{array}{c} = 3 \\ \left\{ \begin{array}{l} g_8(3) = 120 \end{array} \right. \end{array}$$

iii

$R_0 = 56 \Rightarrow$ 第 57 個，又，由題目所附之排序順序：

時間



\therefore The cost of each symbol: 00001101

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