2008 Advanced Coding Theorem HW#2 Due date :2008.04.11

1. Let C be the LDPC code given by the null space of H, which is

$$\mathbf{H} = \begin{bmatrix} 1 & 1 & 0 & 1 & 0 & 0 & 0 \\ 0 & 1 & 1 & 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 1 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 & 1 & 0 & 1 \\ 1 & 0 & 0 & 0 & 1 & 1 & 0 \\ 0 & 1 & 0 & 0 & 0 & 1 & 1 \\ 1 & 0 & 1 & 0 & 0 & 0 & 1 \end{bmatrix}$$

- (a) Please find out the minimum distance of C.
- (b) Please construct the bipartite graph of C.
- (c) Does the bipartite graph of this code contain cycles of 4?
- (d) Determine the number of cycles of length 6 in the graph.
- 2. Consider LDPC code with

$$\mathbf{H} = \begin{bmatrix} 1 & 1 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 1 & 1 \\ 1 & 0 & 1 & 0 & 1 & 0 \\ 0 & 1 & 0 & 1 & 0 & 1 \end{bmatrix}$$

The initial message is $\{u_v^{(0)}\} = \{1.3, -0.9, 0.2, -0.2, -1.1, -0.4\}$

Do SPA (Sum-Product Algorithm) with the maximum number of iterations I_{max} =3.